

ج بخش-۳ شماره تمرین

$$\text{Sum}[r^{2n} e^{i 2 n k L}, \{n, 0, \infty\}]$$

$$= \frac{1}{-1 + e^{2 i k L} r^2}$$

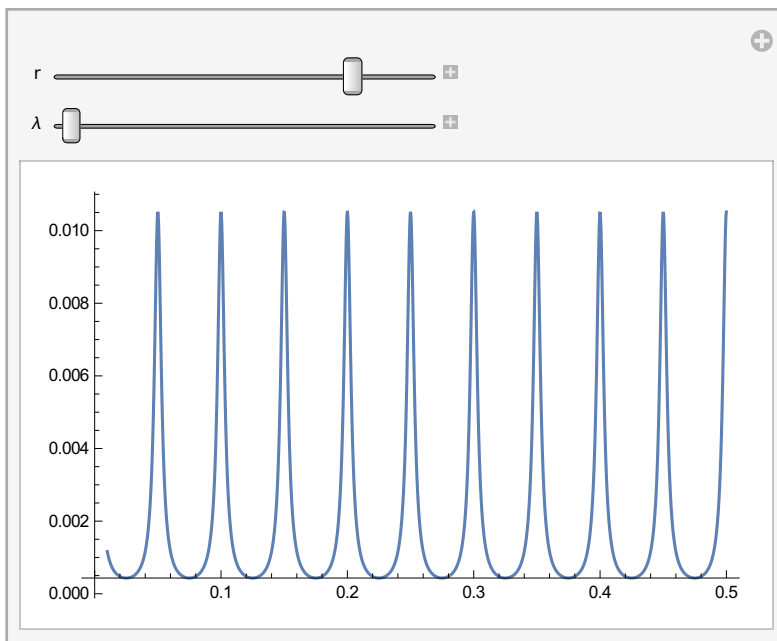
$$\text{Sum}[\alpha^n, \{n, 0, \infty\}]$$

$$\frac{1}{1 - \alpha}$$

ورودی موج طول و انعکاس ضریب مقدار توانید می زیر نمودار در

$$\text{Manipulate}[\text{With}[\{k = 2 \pi / \lambda\},$$

$$\text{Plot}[\text{Abs}[\frac{(1-r)^2}{-1 + e^{2 i k L} r^2}]^2, \{L, .1 \lambda, 5 \lambda\}, \text{PlotRange} \rightarrow \{\text{All}, \text{All}\}]], \{r, 0, 1\}, \{\lambda, .1, 1\}]$$



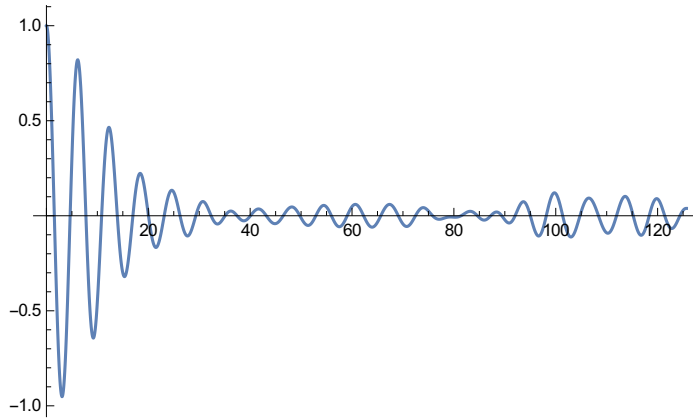
الف بخش-۴ سوال

`nLight = 100; ω_0 = 1; d ω ratio = .1;`

`ω list = Table[RandomVariate[NormalDistribution[ω_0 , d ω ratio * ω_0]], nLight];`

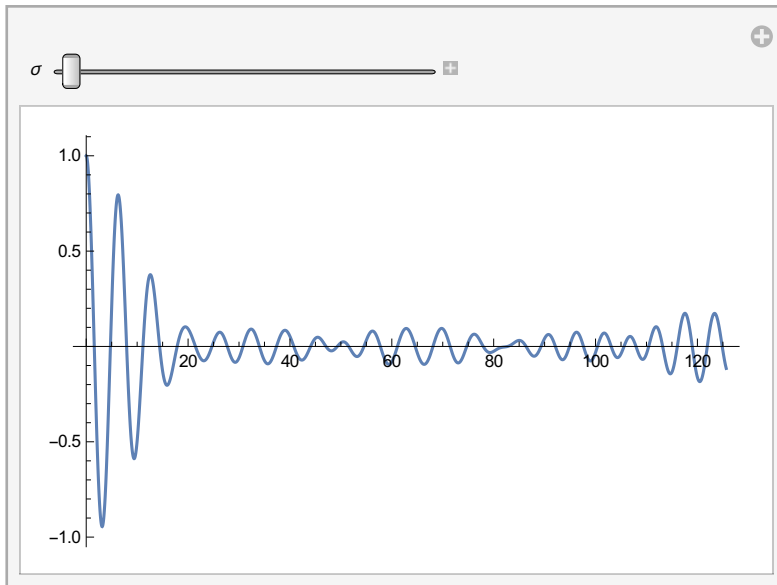
`ϕ list = Table[RandomVariate[NormalDistribution[ϕ_0 , d ϕ ratio * ϕ_0]], nLight];`

```
Plot[1/nLight * Total[Table[Cos[ $\omega$ list[[i]] t(++) $\phi$ list[[i]]*]), {i, 1, nLight}]],  
{t, 0, 40  $\pi$ }, PlotRange -> All]
```



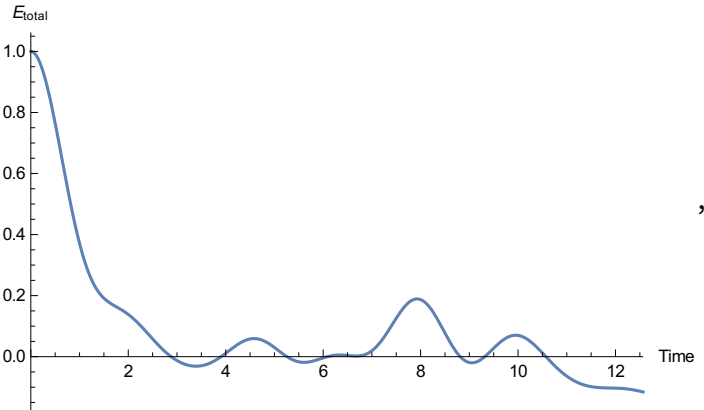
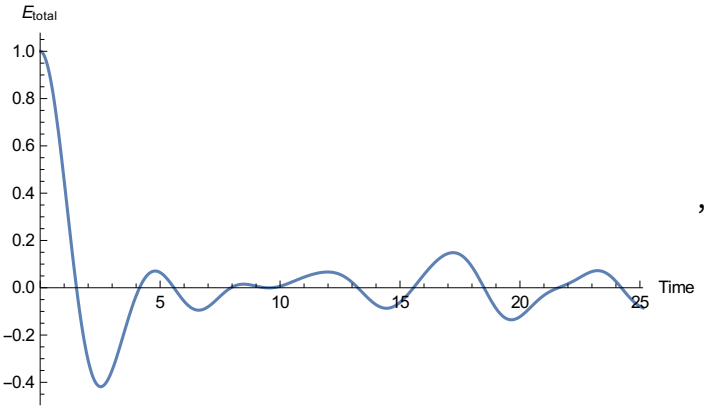
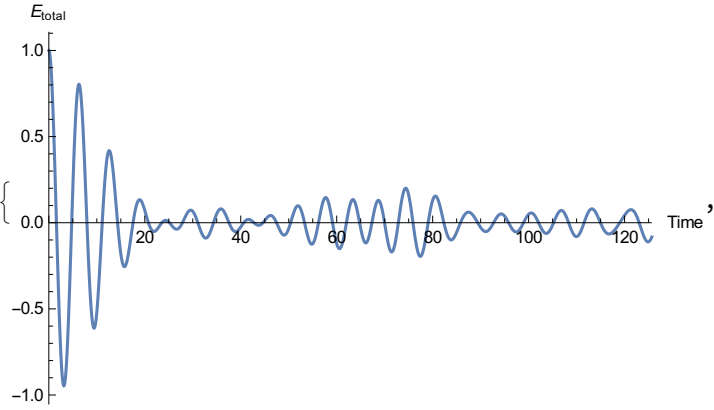
Here you can change σ dynamically and see how that affects the coherence time.

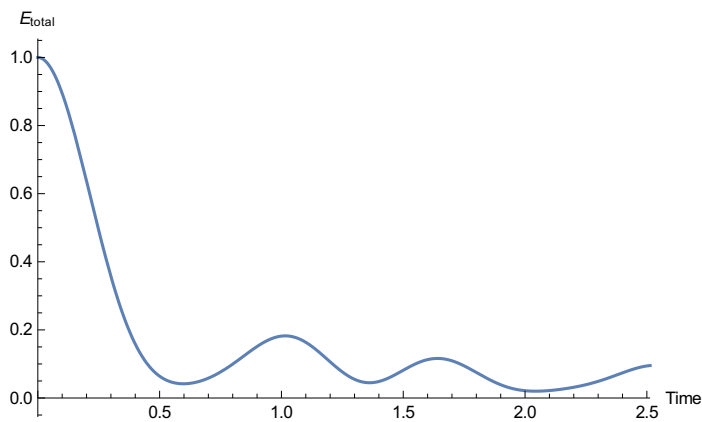
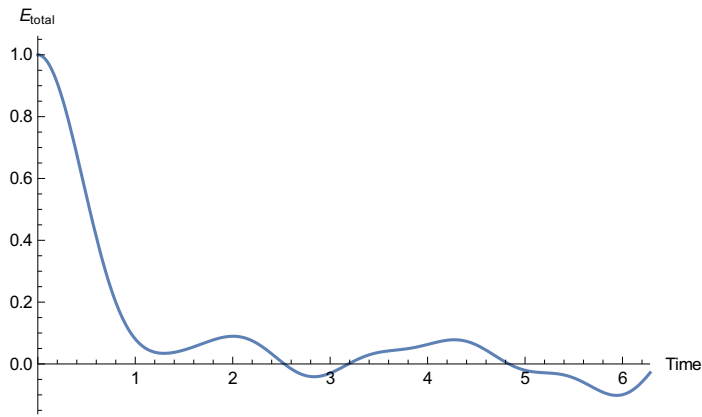
```
Manipulate[  
  With[{ $\omega$ list = Table[RandomVariate[NormalDistribution[ $\omega_0$ , d $\omega$ ratio *  $\omega_0$ ]], nLight] },  
    Plot[1/nLight * Total[Table[Cos[ $\omega$ list[[i]] t], {i, 1, nLight}]],  
    {t, 0, 40  $\pi$ }, PlotRange -> All]], {{d $\omega$ ratio, .1, " $\sigma$ "}, .1, 1}]
```



Net electric field as a function of time for different values of σ

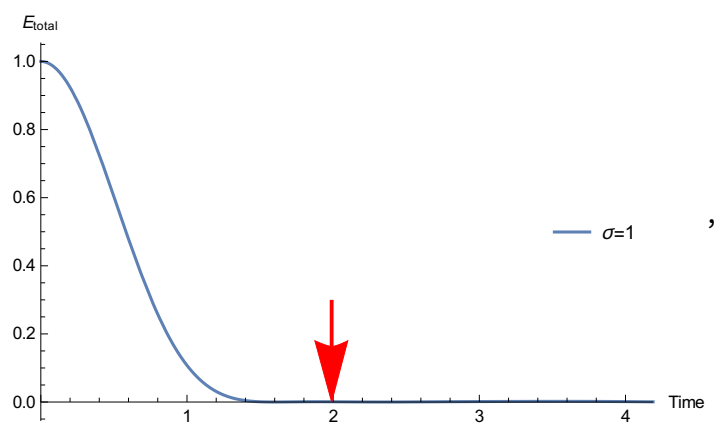
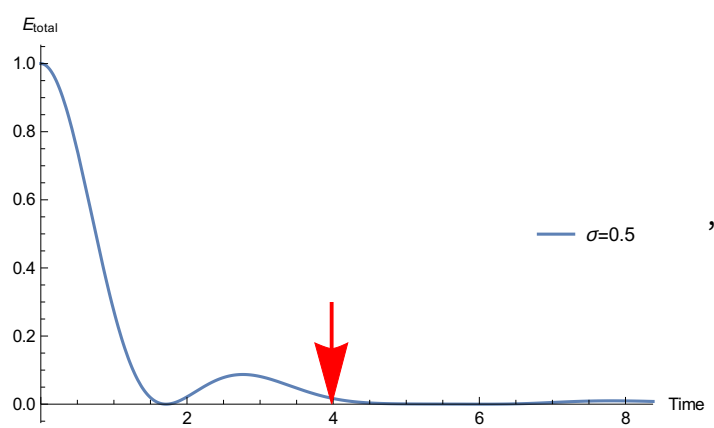
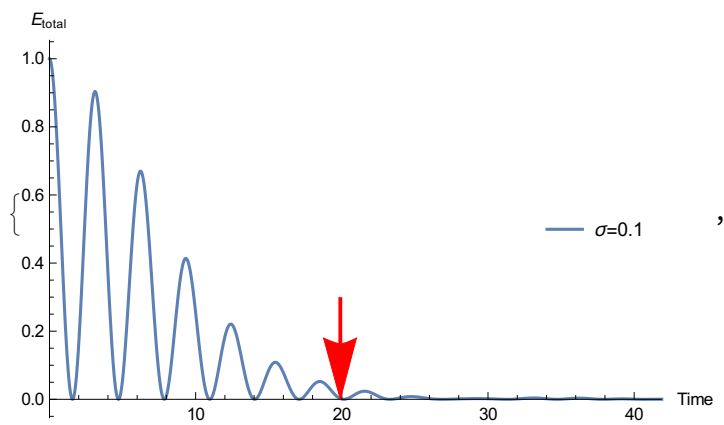
```
Table[  
  With[{ $\omega$ list = Table[RandomVariate[NormalDistribution[ $\omega_0$ , d $\omega$ ratio *  $\omega_0$ ]], nLight] },  
    Plot[1/nLight * Total[Table[Cos[ $\omega$ list[[i]] t], {i, 1, nLight}]],  
    {t, 0, 40  $\pi$  / 10 / d $\omega$ ratio}, PlotRange -> {{0, 40  $\pi$  / 10 / d $\omega$ ratio}, All},  
    ImageSize -> Medium, AxesLabel -> {"Time", "Etotal"}], {d $\omega$ ratio, {.1, .5, 1, 2, 5}}]
```

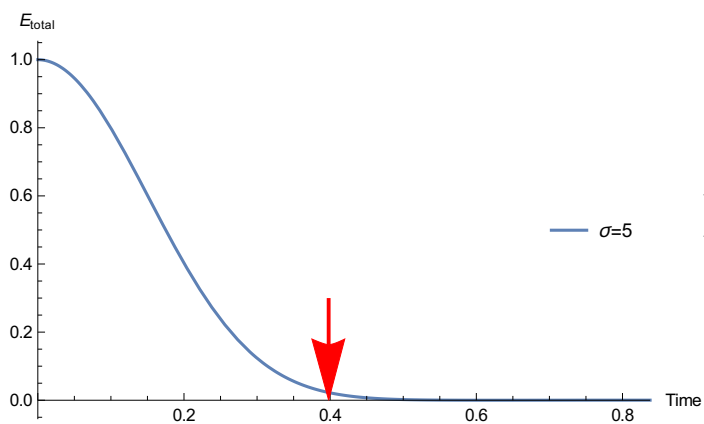
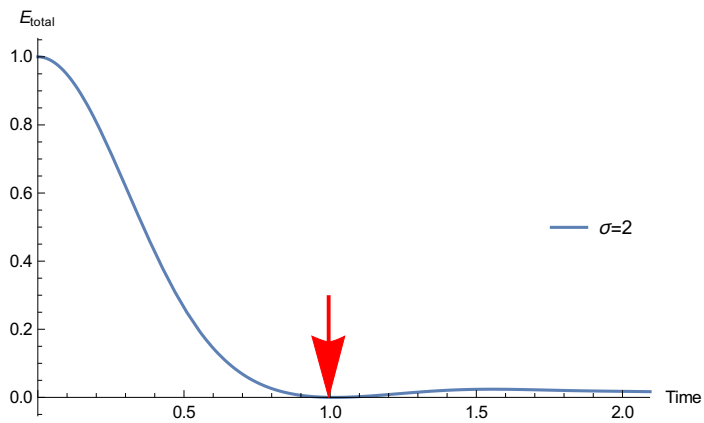




Light intensity as a function of time for different values of σ

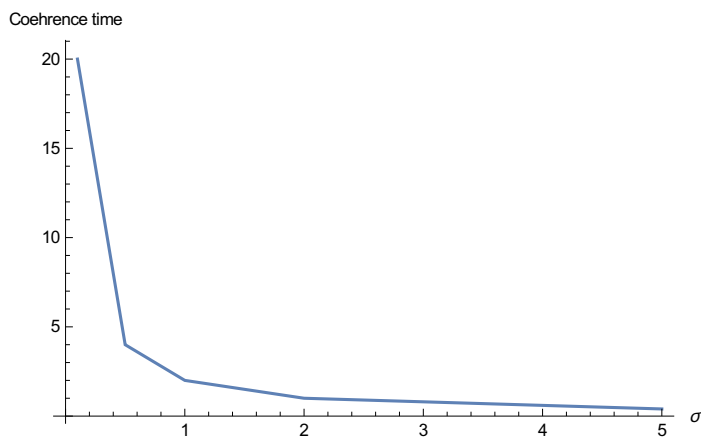
```
Table[
  With[{wlist = Table[RandomVariate[NormalDistribution[w0, dwratio * w0]], nLight] },
    Plot[Abs[1/nLight * Total[Table[Cos[wlist[[i]] t], {i, 1, nLight}]]]^2,
      {t, 0, 40 π / 30 / dwratio}, PlotRange -> {{0, 40 π / 30 / dwratio}, All},
      ImageSize -> Medium, PlotLegends -> Placed[{"σ=" <> ToString[dwratio]},
        {Right, Center}], AxesLabel -> {"Time", "E_total"},
      Epilog -> {Arrowheads[.1], Thick, Red, Arrow[{19 π / 30 / dwratio, .3},
        {19 π / 30 / dwratio, 0}]}], {dwratio, {.1, .5, 1, 2, 5}}]
```





Here's the list of the points indicated in the plots above which represent the coherence time. The following plot shows how the coherence time decreases with widening the uncertainty range in frequency.

```
 $\sigma$ list = {{.1, 20}, {.5, 4}, {1, 2}, {2, 1}, {5, .4}};
ListPlot[ $\sigma$ list, Joined → True, AxesLabel → {" $\sigma$ ", "Coehrence time"}]
```



In a log log plot, it is clear that this is a power-law.

```
ListLogLogPlot[ $\sigma$ list, Joined  $\rightarrow$  True,  
AxesLabel  $\rightarrow$  {" $\sigma$ ", "Coehrence time"}, PlotMarkers  $\rightarrow$  {Automatic, 10}]
```

